

p. 153 #14

$$y = (\csc x + \cot x)^{-1} \quad \frac{dy}{dx}$$

$$\frac{dy}{dx} = -1(\csc x + \cot x)^{-2} \cdot (-\csc x \cot x - \csc^2 x)$$

$$= \frac{\csc x \cot x + \csc^2 x}{(\csc x + \cot x)^2}$$

$$= \frac{\csc x (\cot x + \csc x)}{(\cot x + \csc x)^2}$$

$$= \frac{\csc x}{\cot x + \csc x}$$

$$\#17 \quad y = \sin^3 x \cdot \tan 4x$$

$$y = (\sin x)^3 \cdot \tan(4x)$$

$$u = (\sin x)^3 \quad v = \tan(4x)$$

$$u' = 3\sin^2 x \cos x \quad v' = \sec^2(4x) \cdot 4 = 4\sec^2(4x)$$

$$\frac{dy}{dx} = u'v + uv' \quad \text{product}$$

$$= 3\sin^2 x \cos x \tan 4x + 4\sin^3 x \sec^2 4x$$

$$= \sin^2 x (3 \cos x \tan 4x + 4 \sin x \sec^2 4x)$$

p. 162 #1

$$x^2 y + x y^2 = 6 \quad \text{find } \frac{dy}{dx}$$

$$2x \cdot y + x^2 \cdot \frac{dy}{dx} + 1 \cdot y^2 + x \cdot 2y \cdot \frac{dy}{dx} = 0$$

$$\begin{array}{ll} u = x^2 & v = y \\ u' = 2x & v' = \frac{dy}{dx} \end{array} \quad \begin{array}{ll} u = x & v = y^2 \\ u' = 1 & v' = 2y \cdot \frac{dy}{dx} \end{array}$$

$$x^2 \frac{dy}{dx} + 2xy \frac{dy}{dx} = -2xy - y^2$$

$$\frac{dy}{dx} (x^2 + 2xy) = -2xy - y^2$$

$$\frac{dy}{dx} = \frac{-2xy - y^2}{2xy + x^2} = -\frac{2xy + y^2}{2xy + x^2}$$